

## Function in Vertex Form

Let's take a closer look at the equation,  $y = (x - 2)^2 - 5$ .

First, what are the values for  $p$  &  $q$  in this equation?

Now look at the vertex. What do you notice about its  $(x, y)$  values?

They appear to be the same as the values for  $p$  &  $q$ .

Let's look at the another equation that we examined earlier,  $y = (x + 3)^2 - 1$

This function can also be stated as  $y = (x - - 3)^2 - 1$

{say it as:  $y = (x \text{ minus negative } 3)^2 - 1$ } ...to match this form of the function.

Can we find the same pattern in this example?

What are  $p$  &  $q$  in this equation?

Are these two values also found at the vertex?

It looks like once again, the  $(x, y)$  values of the vertex are the same as the values for  $p$  &  $q$ .

Do you wonder why they are the same?

We can find out by understanding the horizontal and vertical translations.

Let's begin with the basic function  $y = x^2$ .

Its vertex is at the origin,

How many units and in what direction along the  $x$ -axis has the function

$y = (x \text{ minus negative } 3)^2 - 1$  moved?

... how many units and in what direction along the  $y$ -axis has the function moved?

So what must the  $(x, y)$  values at its new vertex be?

The  $(x, y)$  values at the vertex of the basic function are  $(0, 0)$ .

The function  $y = (x - p)^2 + q$  moves  $p$  units along the  $x$ -axis

... and  $q$  units along the  $y$ -axis

So the  $(x, y)$  values at the vertex must be  $p$  and  $q$ .

Now we can see why  $p$  &  $q$  are always the  $(x, y)$  values at the vertex of the function

$$y = (x - p)^2 + q.$$