

Function in Vertex Form

Let's take a closer look at the equation, $y = (x - 2)^2 - 5$.

First, what are the values for p & q in this equation?

Now look at the vertex. What do you notice about its (x, y) values?

They appear to be the same as the values for p & q .

Let's look at the another equation that we examined earlier, $y = (x + 3)^2 - 1$

This function can also be stated as $y = (x - - 3)^2 - 1$

{say it as: $y = (x \text{ minus negative } 3)^2 - 1$ } ...to match this form of the function.

Can we find the same pattern in this example?

What are p & q in this equation?

Are these two values also found at the vertex?

It looks like once again, the (x, y) values of the vertex are the same as the values for p & q .

Do you wonder why they are the same?

We can find out by understanding the horizontal and vertical translations.

Let's begin with the basic function $y = x^2$.

Its vertex is at the origin,

How many units and in what direction along the x -axis has the function

$y = (x \text{ minus negative } 3)^2 - 1$ moved?

... how many units and in what direction along the y -axis has the function moved?

So what must the (x, y) values at its new vertex be?

The (x, y) values at the vertex of the basic function are $(0, 0)$.

The function $y = (x - p)^2 + q$ moves p units along the x -axis

... and q units along the y -axis

So the (x, y) values at the vertex must be p and q .

Now we can see why p & q are always the (x, y) values at the vertex of the function

$$y = (x - p)^2 + q.$$